

Modelling vaccine escape in a population

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Vaccination campaigns and antigenic escape strains

Might vaccination campaigns unintendedly select for pathogen strains that escape host immunity?

Epidemiological and evolutionary considerations of SARS-CoV-2 vaccine dosing regimes

Chadi M. Saad-Roy^{1*}, Sinead E. Morris², C. Jessica E. Metcalf^{3,4}, Michael J. Mina⁵, Rachel E. Baker³,
Jeremy Farrar⁷, Edward C. Holmes⁸, Oliver G. Pybus⁹, Andrea L. Graham³, Simon A. Levin³,
Bryan T. Grenfell^{3,4,10*}, Caroline E. Wagner^{11*}

Rates of SARS-CoV-2 transmission and vaccination impact the fate of vaccine-resistant strains

Simon A. Rella¹, Yuliya A. Kulikova², Emmanouil T. Dermitzakis³ & Fyodor A. Kondrashov¹

What's the balance between transmission-reduction and a potential selection increase?

Vaccine escape in a heterogeneous population insights for SARS-CoV-2 from a simple model

Julia R. Gog^{1,2}, Edward M. Hill^{2,3,4,5}, Leon Danon and Robin N. Thompson^{2,3,4}

Approach and talk plan

1. Selection during an epidemic



Paper

Gutierrez, M. A. and Gog, J. R.
The importance of vaccinated
individuals to population-level
evolution of pathogens. 2023,
Journal of Theoretical Biology.

2. New epidemic: escape strain



Current work, unpublished

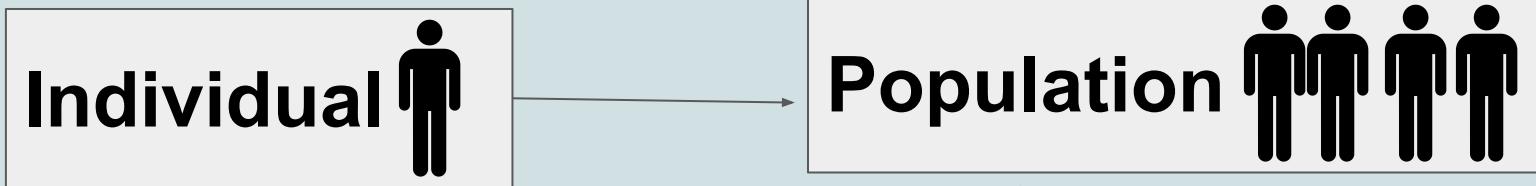
3. Discussion: applications & future work



Simplified scales of selection

not explicitly within-host,
but vaccination status matters!

generation of strains,
(emergence not yet)



$$P(t) \propto (I_U(t) + \theta_E I_V(t))$$

Escape pressure

infections in
unvaccinated hosts

infections in
vaccinated hosts

Relative selection
in vaccinated hosts

Others use just I_V or I_U or a fixed linear combination.

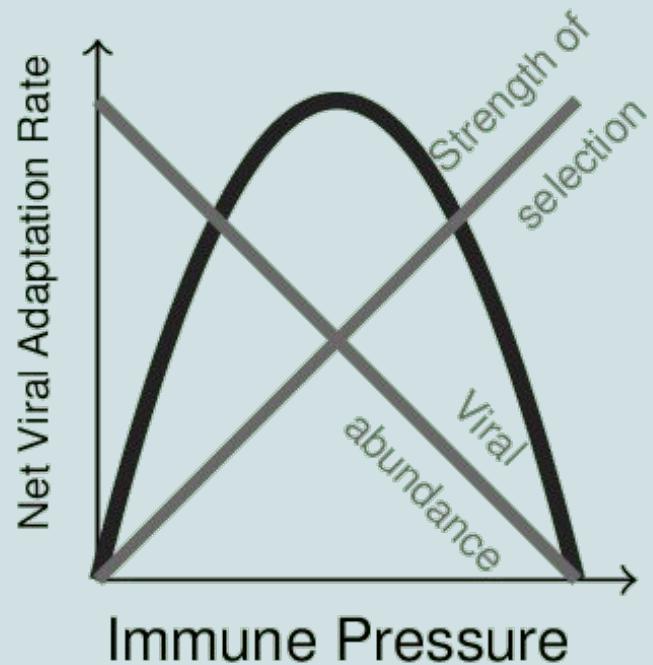
Gog et al 2021, Saad-Roy et al 2021, Thompson et al 2021, Rella et al 2021, Zhang et al 2022

Within-host selection by vaccination status

$$P(t) = I_U(t) + \theta_E I_V(t)$$

$\theta_E > 1?$

If infected, **who is more likely to generate an escape strain?**
Vaccinated or unvaccinated?



Grenfell et al, Science 2004

Transient SIR epidemic wave

vaccination coverage c :

vaccines given before outbreak,
permanent partial immunity
against infection θ_S and transmission θ_I

Initial
conditions

$$S_U(0) = 1 - c$$

$$S_V(0) = c\theta_S$$

Polarised
protection
against infection

$$\dot{S}_U = -S_U \lambda$$

Force of infection

$$\dot{S}_V = -S_V \lambda$$

$$\lambda = R_0(I_U + \theta_I I_V)$$

reduced
transmissibility

$$\dot{I}_U = S_U \lambda - I_U$$

$$\dot{I}_V = S_V \lambda - I_V$$

SIR dynamics

Further assumptions:
well-mixing,
homogeneity,
no reinfections,
constant R_0 ,
not time-since-infection,
same infectious period,
no births and deaths.

Analytical final-size solution leads to escape pressure

Initial effective R-number $R_e = R_0(1 - c(1 - \theta_S \theta_I))$

vaccine transmission-blocking

Same ratio vaccinated:unvaccinated through all compartments

$$(S_V, I_V, R_V) = \frac{c\theta_S}{1-c} (S_U, I_U, R_U)$$

Integrated escape pressure $P = \int_0^\infty (I_U + \theta_E I_V) dt = C_U + \theta_E C_V$

...similar to standard SIR final-size

Cumulative final-sizes

$$P = (1 - c(1 - \theta_S \theta_E))(1 + R_e^{-1} W(-R_e e^{-R_e}))$$

"escape-blocking factor"

Lambert W function

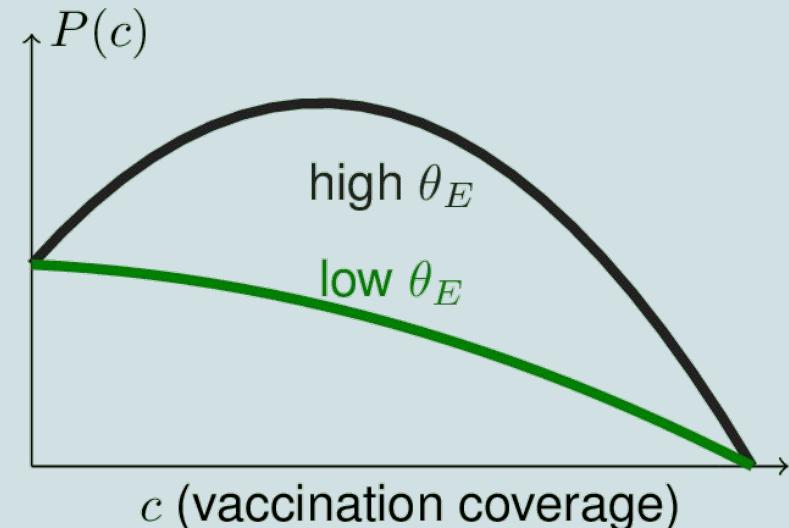
Escape pressure P as a function of vaccination coverage c

$$P = C_U + \theta_E C_V$$

Behaviour of P depends on the relative escape contribution of vaccinees, θ_E

- Unimodal if θ_E above threshold
- Decreasing if θ_E below threshold

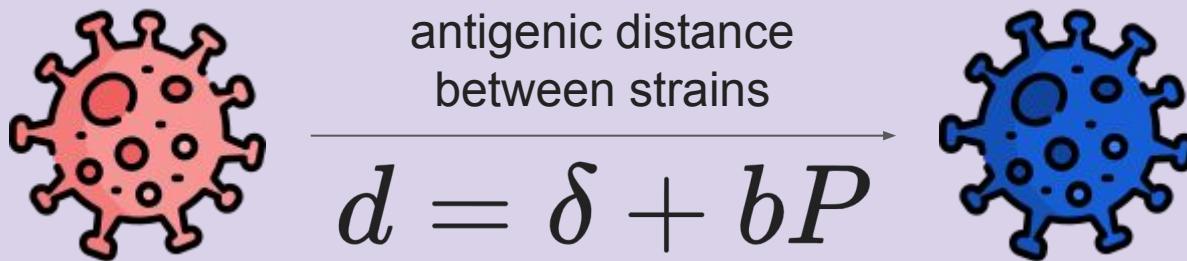
P always decreases to zero if vaccination coverage is near herd immunity threshold



Gutierrez and Gog, 2023, *JTB*

What are the consequences of a high escape pressure?

After the first epidemic wave, a new escape strain generates a 2nd epidemic wave



The antigenic distance is linear on the escape pressure, $P = C_U + \theta_E C_V$ so includes infections in both vaccinated and unvaccinated, weighted by θ_E

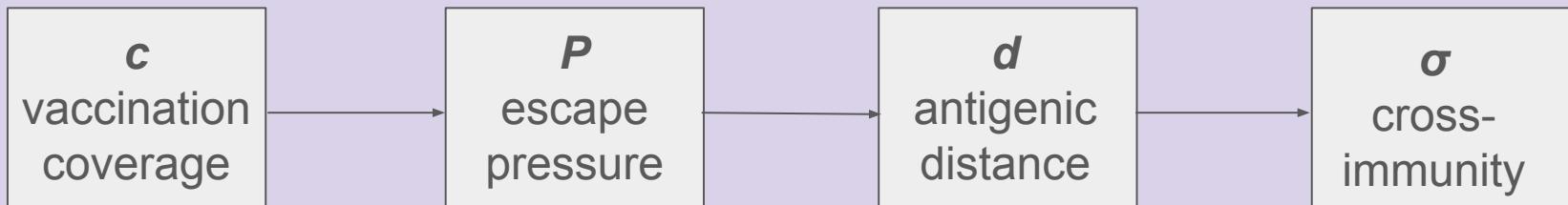
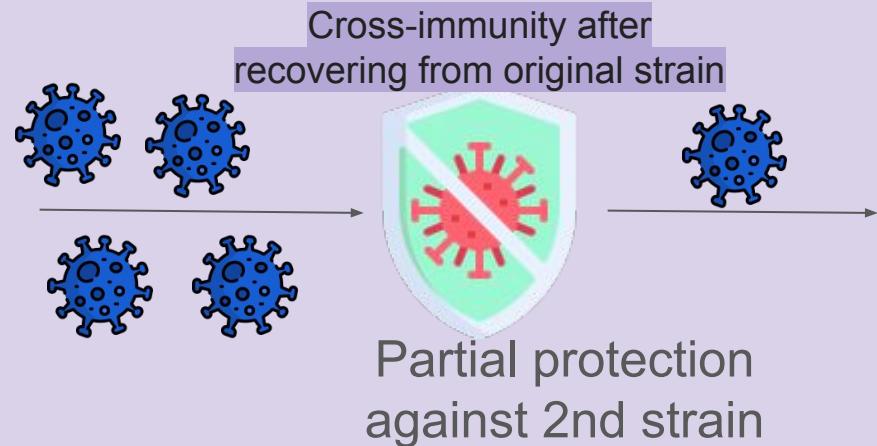
Adapted to include vaccination from Boni et al 2004 ($d = \delta + bC$ using total infections C)

Unpublished work, in preparation for PhD thesis

The antigenic distance determines the cross-immunity

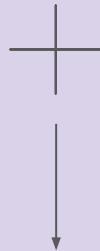
Cross-immunity between strains decays exponentially with the antigenic distance

$$\sigma = \exp(-ad) \quad \text{Boni et al 2004}$$



Total infections C as a function of vaccination coverage c

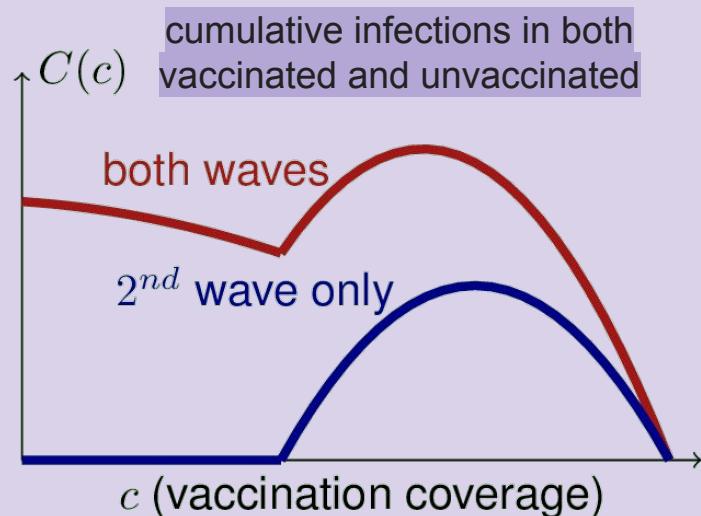
1st wave:
decreasing



2nd wave:
unimodal
(large θ_E)

Total infections (both waves):

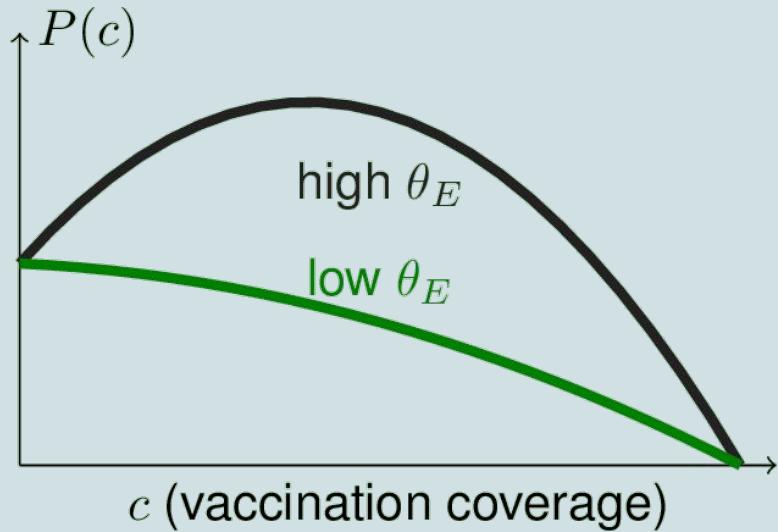
1. initially decreasing (no 2nd wave)
2. increasing as 2nd wave becomes possible
3. local maximum at intermediate vaccination
4. decreases for large vaccination coverages



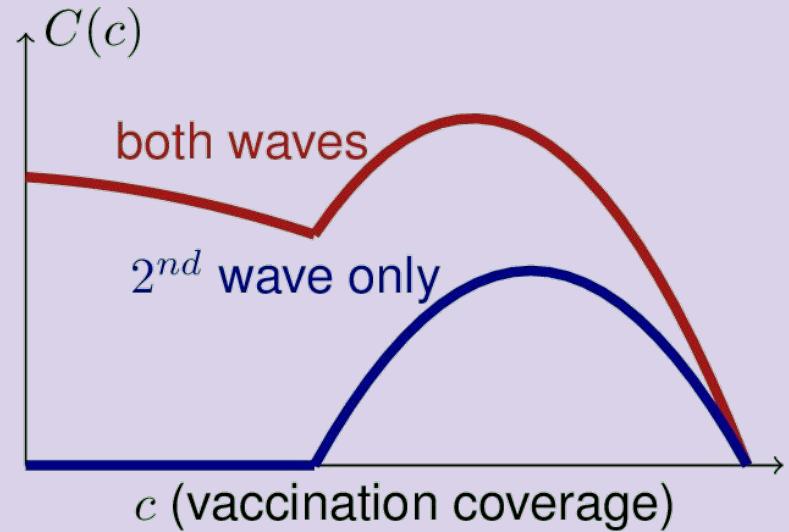
Caveat: slightly different overall balance depending on the drift rate a for the cross-immunity $\sigma = \exp(-ad)$

Summary

Total **escape pressure** from a single epidemic wave, without escape strain.



Total **infections** including a second epidemic wave with an escape strain.



Escape risk and total infections may be highest at intermediate vaccination.

Applications and work in progress

Vaccination strategies & surveillance...

eg, saving some vaccine doses for the second wave



Heterogeneous population & immunocompromised hosts

Reinfections during the first wave & infection-acquired immunity versus vaccines

Stochastic invasion dynamics of the escape strain

Further epidemic evolution?



What is the value of θ_E and the drift rate a (eg, for SARS-CoV-2, Influenza)?

Extras

Immunity assumptions for second strain

Cross-immunity protects (partially) against *infection*

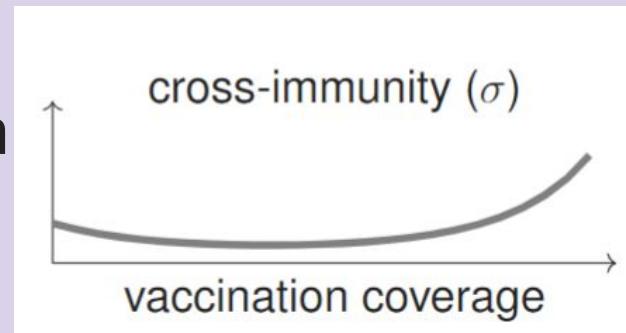
in vaccinees and hosts recovered from the first strain

Conserved vaccine efficacy (VE) against *transmission*

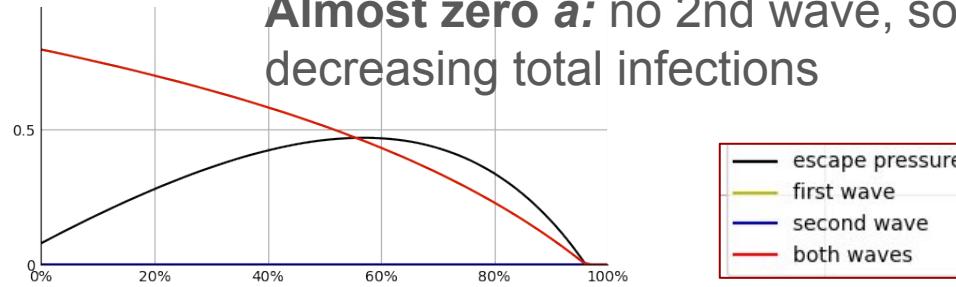
Increasing the vaccination coverage...

- Fewer hosts infected with the first strain, so now more susceptible hosts
- Non-monotonic effects on the cross-immunity (“U-shaped”)
- Reduces transmission through the VE against transmission

Overall balance of vaccination effects for 2nd wave: a priori unclear

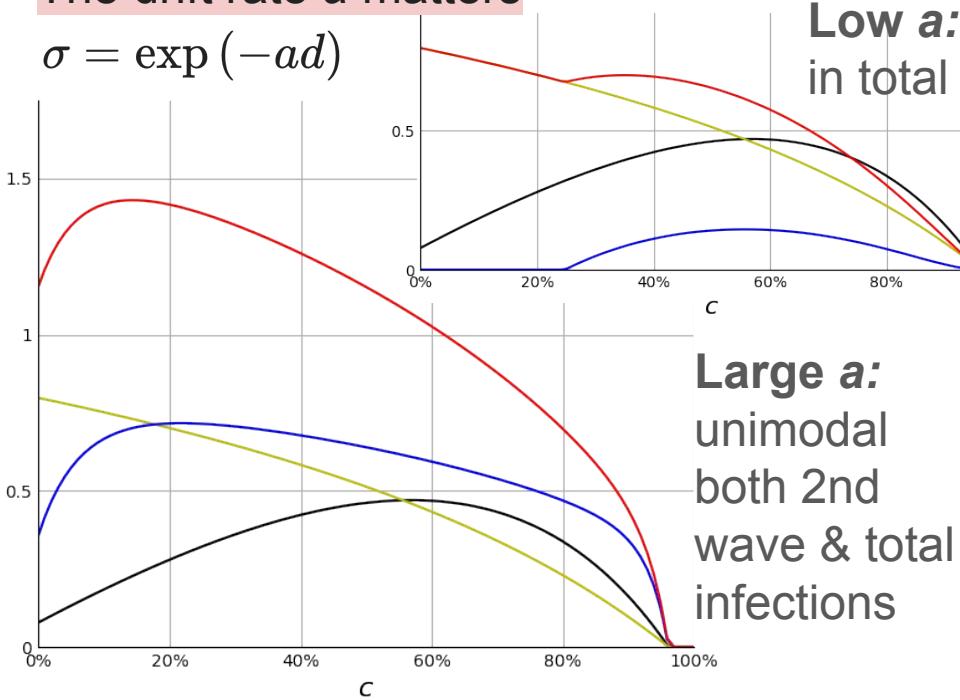


Almost zero a : no 2nd wave, so decreasing total infections



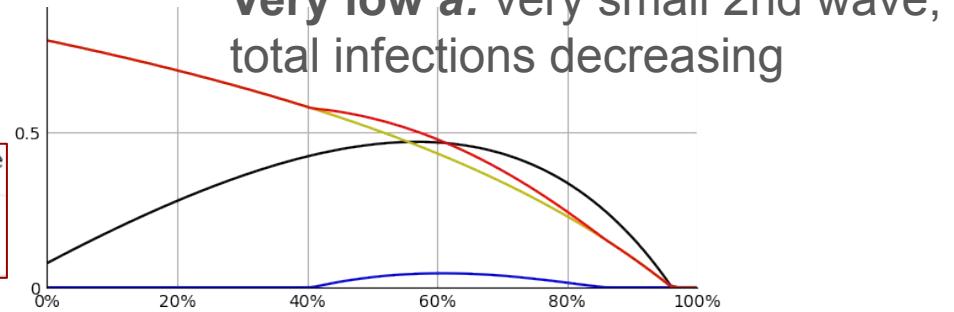
The drift rate a matters

$$\sigma = \exp(-ad)$$

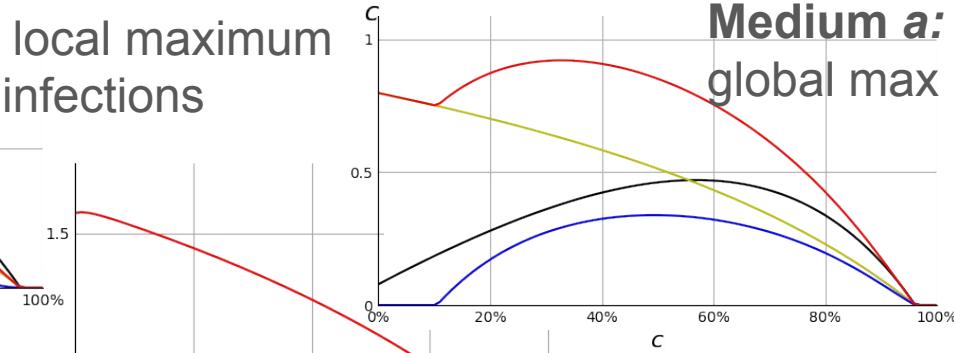


Large a :
unimodal
both 2nd
wave & total
infections

Very low a : very small 2nd wave,
total infections decreasing



Medium a :
global max



Very large a :
decreasing
both 2nd
wave & total
infections

