

Modelling vaccine escape in a population

Maria A. Gutierrez

PhD candidate, with Julia Gog at DAMTP



UNIVERSITY OF
CAMBRIDGE

Vaccination campaigns and antigenic escape strains

Might vaccination campaigns unintendedly select for pathogen strains that escape host immunity?

What's the balance between transmission-reduction and a potential selection increase?

Epidemiological and evolutionary considerations of SARS-CoV-2 vaccine dosing regimes

Chadi M. Saad-Roy^{1*}, Sinead E. Morris², C. Jessica E. Metcalf^{3,4}, Michael J. Mina⁵, Rachel E. Baker³, Jeremy Farrar⁷, Edward C. Holmes⁸, Oliver G. Pybus⁹, Andrea L. Graham³, Simon A. Levin³, Bryan T. Grenfell^{3,4,10*}, Caroline E. Wagner^{11*}

Rates of SARS-CoV-2 transmission and vaccination impact the fate of vaccine-resistant strains

Simon A. Rella¹, Yuliya A. Kulikova², Emmanouil T. Dermitzakis³ & Fyodor A. Kondrashov¹

Vaccine escape in a heterogeneous population insights for SARS-CoV-2 from a simple model

Julia R. Gog^{1,2}, Edward M. Hill^{2,3,4,5}, Leon Danon and Robin N. Thompson^{2,3,4}

Approach and talk plan

1. Selection during an epidemic



Paper

Gutierrez, M. A. and Gog, J. R.
The importance of vaccinated individuals to population-level evolution of pathogens. 2023, *Journal of Theoretical Biology*.

2. New epidemic: escape strain



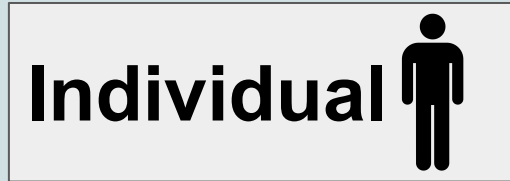
Current work, unpublished

3. Discussion: applications & future work



Simplified scales of selection

not explicitly within-host,
but vaccination status matters!



$$P(t) \propto (I_U(t) + \theta_E I_V(t))$$

Escape pressure infections in unvaccinated hosts θ_E infections in vaccinated hosts

Relative selection
in vaccinated hosts

Others use just I_V or I_U or a fixed linear combination.

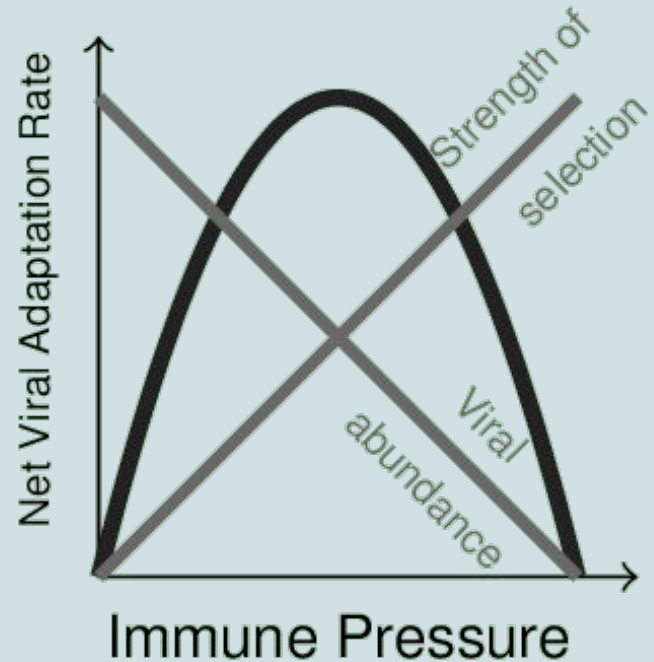
Gog et al 2021, Saad-Roy et al 2021, Thompson et al 2021, Rella et al 2021, Zhang et al 2022

Within-host selection by vaccination status

$$P(t) = I_U(t) + \theta_E I_V(t)$$

$\theta_E > 1?$

If infected, who is more likely to generate an escape strain?
Vaccinated or unvaccinated?



Grenfell et al, Science 2004

Transient SIR epidemic wave

vaccination coverage c :
vaccines given before outbreak,
permanent partial immunity
against infection θ_S and transmission θ_I

Initial
conditions

$$S_U(0) = 1 - c$$

$$S_V(0) = c\theta_S$$

Polarised protection
against infection

$$\dot{S}_U = -S_U\lambda$$

Force of infection

$$\dot{S}_V = -S_V\lambda$$

$$\lambda = R_0(I_U + \theta_I I_V)$$

reduced
transmissibility

$$\dot{I}_U = S_U\lambda - I_U$$

$$\dot{I}_V = S_V\lambda - I_V$$

SIR dynamics

Further assumptions:
well-mixing,
homogeneity,
no reinfections,
constant R_0 ,
not time-since-infection,
same infectious period,
no births and deaths.

Analytical final-size solution leads to escape pressure

Initial effective R-number $R_e = R_0 (1 - c(1 - \theta_S \theta_I))$

vaccine transmission-blocking

Same ratio vaccinated:unvaccinated through all compartments

$$(S_V, I_V, R_V) = \frac{c\theta_S}{1-c} (S_U, I_U, R_U)$$

Integrated escape pressure $P = \int_0^\infty (I_U + \theta_E I_V) dt = C_U + \theta_E C_V$

...similar to standard SIR final-size

Cumulative final-sizes

$$P = (1 - c(1 - \theta_S \theta_E)) (1 + R_e^{-1} W(-R_e e^{-R_e}))$$

“escape-blocking factor”

Lambert W function

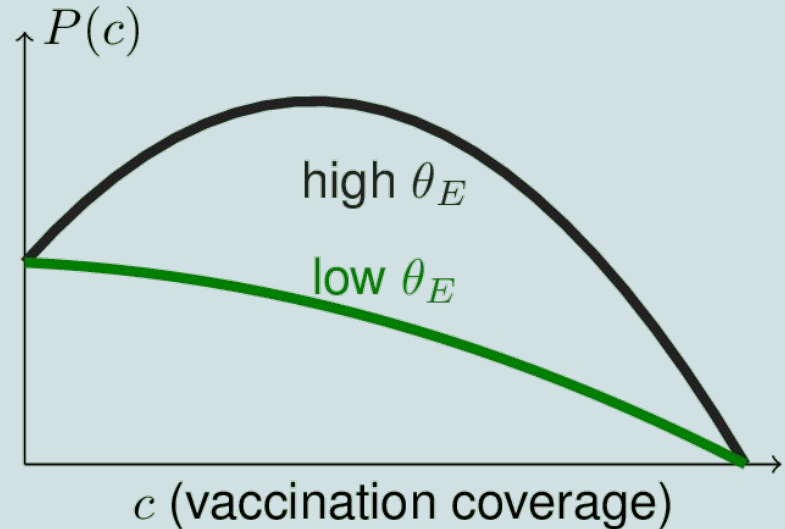
Escape pressure P as a function of vaccination coverage c

$$P = C_U + \theta_E C_V$$

Behaviour of P depends on the relative escape contribution of vaccinees, θ_E

- Unimodal if θ_E above threshold
- **Decreasing** if θ_E below threshold

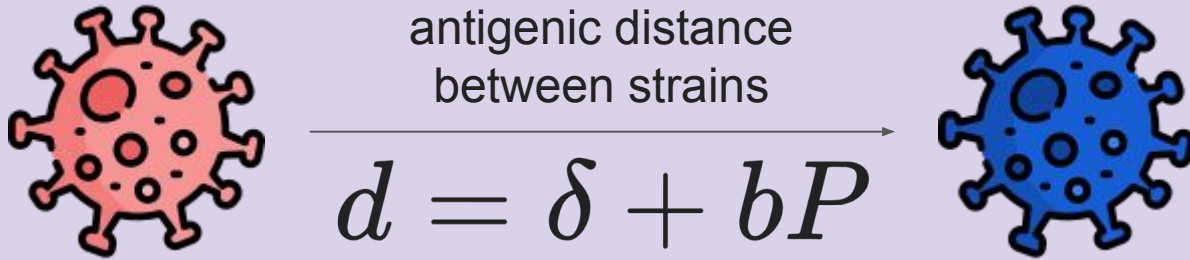
P always decreases to zero if vaccination coverage is near herd immunity threshold



Gutierrez and Gog, 2023, *JTB*

What are the consequences of a high escape pressure?

After the first epidemic wave, a new escape strain generates a 2nd epidemic wave



The antigenic distance is linear on the escape pressure, $P = C_U + \theta_E C_V$ so includes infections in both vaccinated and unvaccinated, weighted by θ_E

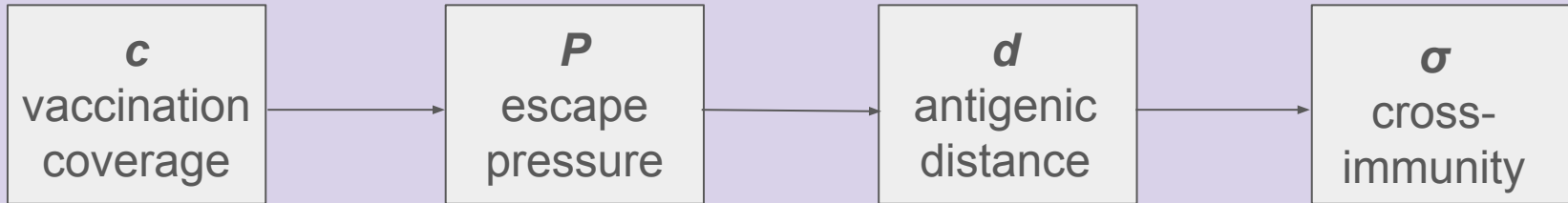
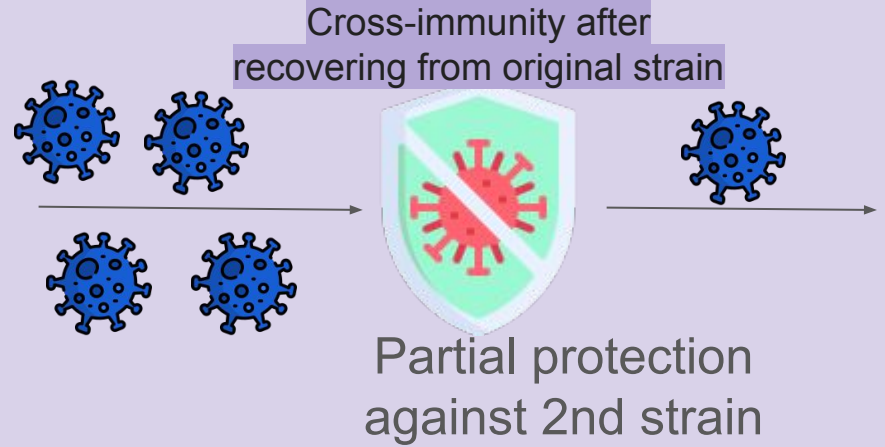
Adapted to include vaccination from Boni et al 2004 ($d = \delta + bC$ using total infections C)

Unpublished work, in preparation for PhD thesis

The antigenic distance determines the cross-immunity

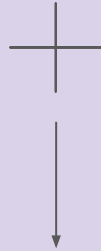
Cross-immunity between strains decays exponentially with the antigenic distance

$$\sigma = \exp(-ad) \text{ Boni et al 2004}$$



Total infections C as a function of vaccination coverage c

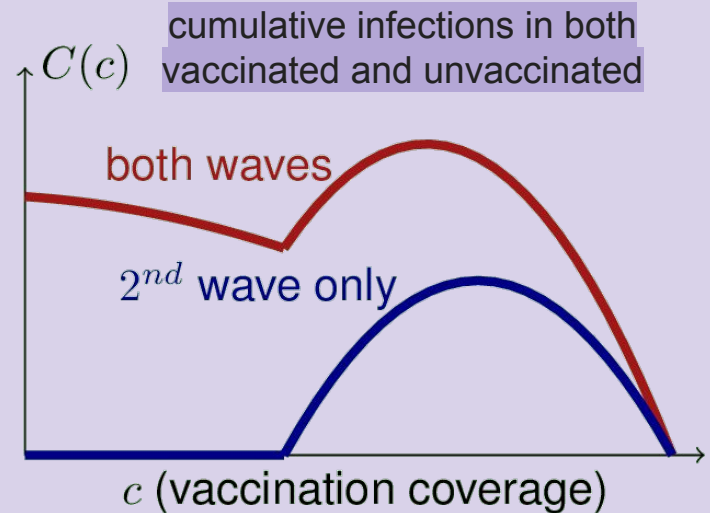
1st wave:
decreasing



2nd wave:
unimodal
(large θ_E)

Total infections (both waves):

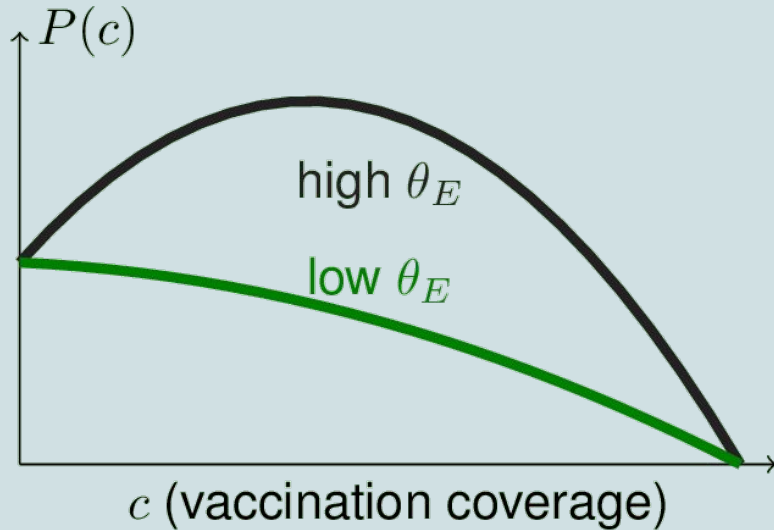
1. initially decreasing (no 2nd wave)
2. increasing as 2nd wave becomes possible
3. local maximum at intermediate vaccination
4. decreases for large vaccination coverages



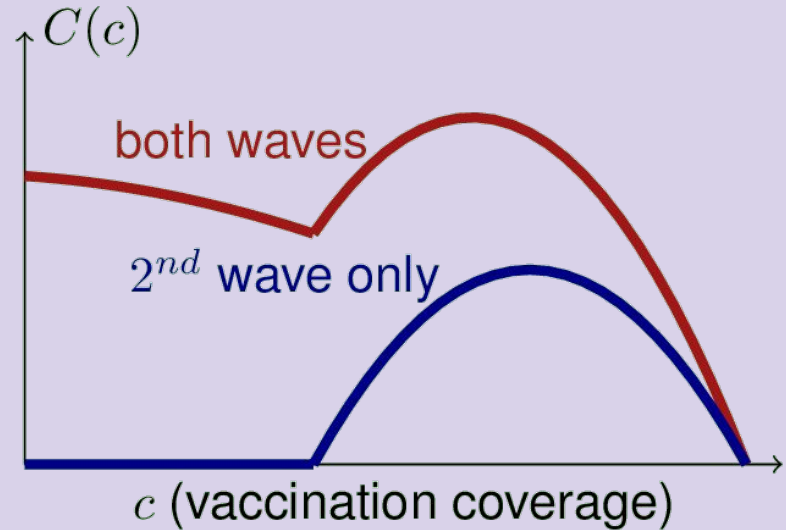
Caveat: slightly different overall balance depending on the drift rate a for the cross-immunity $\sigma = \exp(-ad)$

Summary

Total **escape pressure** from a single epidemic wave, without escape strain.



Total **infections** including a second epidemic wave with an escape strain.



Escape risk and total infections may be highest at intermediate vaccination.

Applications and work in progress

Vaccination strategies & surveillance...

eg, saving some vaccine doses for the second wave



Heterogeneous population & immunocompromised hosts

Reinfections during the first wave & infection-acquired immunity versus vaccines

Stochastic invasion dynamics of the escape strain

Further epidemic evolution?



What is the value of θ_E and the drift rate a (eg, for SARS-CoV-2, Influenza)?

Extras

Immunity assumptions for second strain

Cross-immunity protects (partially) against *infection*

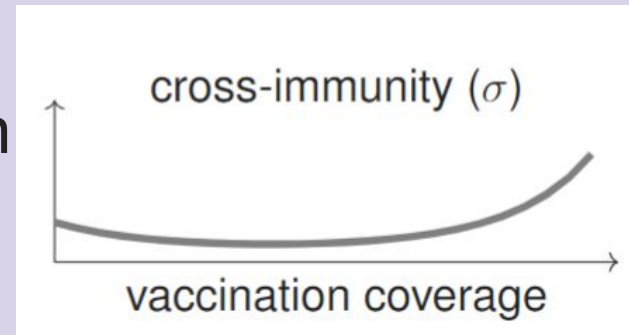
in vaccinees and hosts recovered from the first strain

Conserved vaccine efficacy (VE) against *transmission*

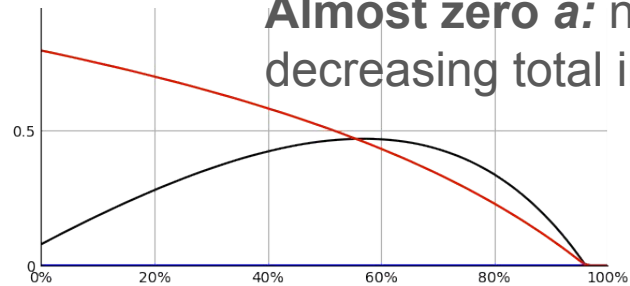
Increasing the vaccination coverage...

- Fewer hosts infected with the first strain, so now more susceptible hosts
- Non-monotonic effects on the cross-immunity (“U-shaped”)
- Reduces transmission through the VE against transmission

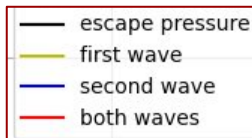
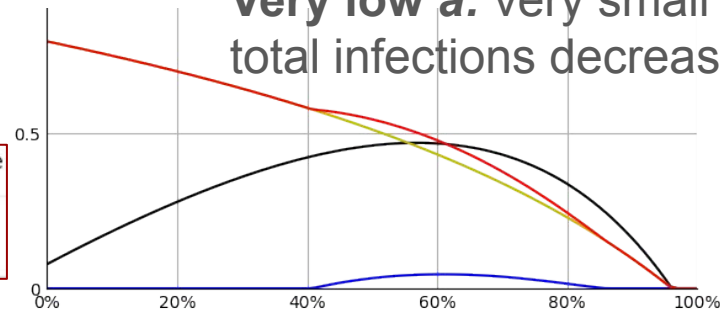
Overall balance of vaccination effects for 2nd wave: a priori unclear



Almost zero a : no 2nd wave, so decreasing total infections



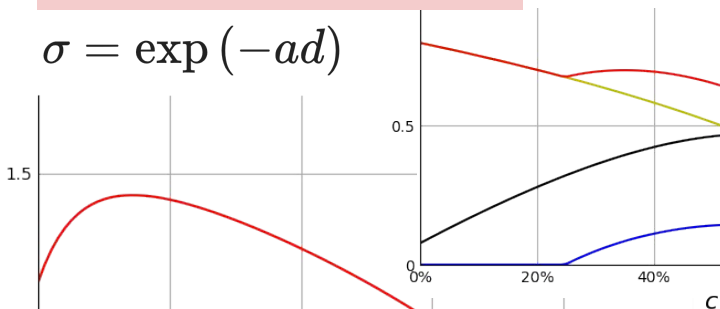
Very low a : very small 2nd wave, total infections decreasing



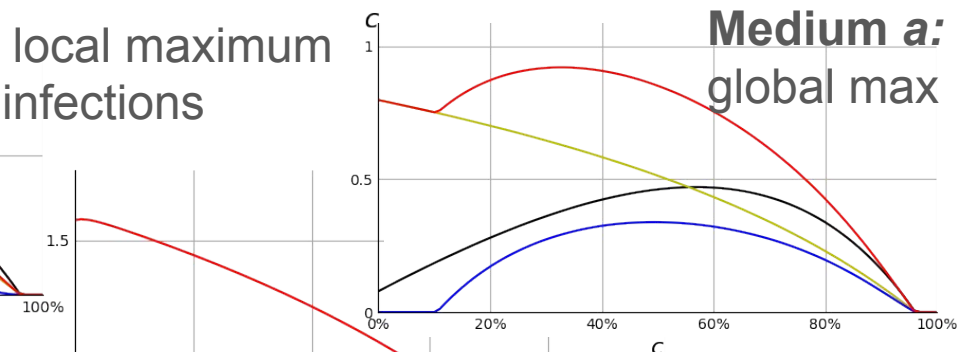
The drift rate a matters

$$\sigma = \exp(-ad)$$

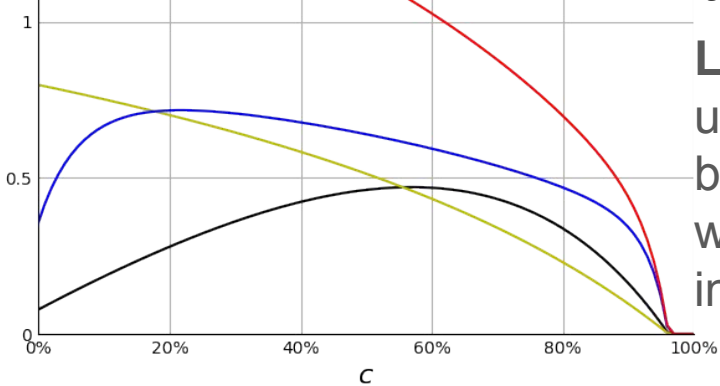
Low a : local maximum in total infections



Medium a : global max



Large a : unimodal both 2nd wave & total infections



Very large a : decreasing both 2nd wave & total infections

